## חATIIBIA UTIVERSITY

OF SCIEMCE AMD TECHMOLOGY

## Faculty of Health and Applied Sciences

Department of Mathematics and Statistics

| QUALIFICATION: Bachelor of Science ; Applied Mathematics and Statistics |  |
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| QUALIFICATION CODE: 07BSAM | LEVEL: 5 |
| COURSE: FINANCIAL MATHEMATICS 1 | COURSE CODE: FIM502S |
| DATE: November 2022 | SESSION: Theory |
| DURATION: 3 Hours | MARKS: 100 |


| FIRST OPPORTUNITY EXAM QUESTION PAPER |  |
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| EXAMINER(S) | Dr Victor Katoma |
|  |  |
| MODERATOR: | Prof Samuel Eegunjobi |

THIS QUESTION PAPER CONSISTS OF 2 PAGES
(Excluding this front page)
INSTRUCTIONS

1. Answer ALL the questions.
2. Write clearly and neatly.
3. Number the answers clearly.

PERMISSIBLE MATERIALS

1. Non-programmable pocket calculator without the cover

## QUESTION 1 (25 MARKS)

1.1 Explain/define the following:
1.1.1 Amortisation of a Loan repayment
(5)
1.1.2 Annuity
1.1.3 Deferred annuity
2.1 Rudy buys a piece of land for $N \$ 110,000$. He makes $20 \%$ down payment and for the balance he takes a loan for 25 years that charges an annual interest rate of $5 \%$ compounded monthly. Find the
1.2.1 Monthly payments
1.2.2 Total amount of interest that will be paid
1.2.3 Amount of the loan that he would have paid after 10 years

## QUESTION 2 (25 MARKS)

2.1 Show that $a_{n]}=\frac{1-(v)^{n}}{i}$
2.2 Mr Kandji has purchased a farm worth N $\$ 50,000$ through the bank. He has decided to pay back the loan in yearly instalments in arrears over 5 years. If money is worth $8 \%$ p.a., schedule these payments on an amortization schedule.
2.3 Use $\boldsymbol{a}_{\boldsymbol{n}}$ to prove that after a third (3) payment the Loan balance is N\$ 22,331.51

## QUESTION 3 (25 MARKS)

3.1 What is time value of money?
(2)
3.2 Anna set up an annuity to save for her retirement. She arranged to have $N \$ 800$ taken out of each of her monthly wages and deposited into this account; it will earn annual interest of 4.5\% compounded monthly. She just had her thirtieth birthday, and her ordinary annuity comes to term when she is sixty-five. Find the following
3.2.1 The future value of the account
3.2.2 Anna's total contribution to the account
3.2.3 The total interest earned
3.4 After making a down payment of $N \$ 4000$ for an automobile, Murphy paid $N \$ 400$ per month for 36 months with interest charged at $\mathrm{j}_{12}=12 \%$ on the unpaid balance

### 3.4.1 What was the original cost of the car?

3.4.2 What part of Murphy's total car payments went toward interest charges?

## QUESTION 4 (25 MARKS)

4.1 At what interest rate (compounded continuously) would an investment $C_{0}$ centuple ( 100 times) in 25 years?
4.2 Prove that $\ddot{S}_{n]}=\frac{(\mathbf{1}+i)^{n}-\mathbf{1}}{d}$
4.3 Define the following

### 4.2.1 Sinking fund

(3)
4.2.2 Perpetuity
4.2.3 Accumulation factor
4.2.4 Force of interest
4.4 Show that $\ddot{a}_{n \mathrm{~J}}=\frac{1-(v)^{n}}{d}$

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\begin{gathered}
\text {--END OF EXAMINATION- } \\
\text { COEP } \\
\text { KALM } \\
\text { GOOD } \\
\text { LUCK }
\end{gathered}
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